Homework #10, Due: 4/3 Math 181 (Discrete Structures), Spring 2024

Problem 1 is worth 4 points, and Problem 2 is worth 6 points, for a total of 10 points. Remember to *show your work* and *explain your answers* on all problems!

- 1. Let $X = \{1, 2, 3\}$. Define a relation R on $X \times X = \{(a, b) : a, b \in X\}$ where (a, b) R(c, d) if and only if a + b = c + d. For example, we have that (2, 2) R(1, 3) since 2 + 2 = 4 = 1 + 3.
 - (a) Explain why R is an equivalence relation.
 - (b) List one element of each equivalence class of R.
- 2. Let $X = \{a, b, c\}$ and let $S \subseteq X^*$ be the set of strings over the alphabet X of length four. For example, three of the elements in S are: *abab*, *acbb*, and *ccbb*.
 - (a) What is #S (the number of elements in S)?
 - (b) Let $S_1 \subseteq S$ be the subset of strings in S that begin with "a." What is $\#S_1$?
 - (c) Let $S_2 \subseteq S$ be the subset of strings in S that end with "bb." What is $\#S_2$?
 - (d) Let $S_3 \subseteq S$ be the subset of strings in S that begin with "a" or end with "bb" (or both). What is $\#S_3$? **Hint**: use the Principle of Inclusion and Exclusion!